

1. Suppose we know that $\lim_{x \rightarrow -2} f(x) = -3$ and $\lim_{x \rightarrow -2} g(x) = 7$. Find the value of

$$\lim_{x \rightarrow -2} \frac{5f(x)\sqrt{g(x)+3}}{11f(x)-g(x)}$$

and justify each step by naming an appropriate Limit Law. (Use names and not numbers — no one knows the numbers.)

2. Evaluate the limit, if it exists.

(a) $\lim_{x \rightarrow -3} \frac{(x+1)^3 + 8}{x+3}$

(b) $\lim_{h \rightarrow 0} \frac{\frac{1}{2+h} - \frac{1}{2}}{h}$

(c) $\lim_{x \rightarrow 1} \frac{x^2 - 4x + 3}{x^2 + x - 2}$

(d) $\lim_{h \rightarrow 0} \frac{\sqrt{5+h} - \sqrt{5}}{h}$

3. Consider the functions

$$f(x) = -|x-1| \quad g(x) = (x-1) \sin\left(\frac{1}{x-1}\right) \quad h(x) = |x-1|$$

- (a) Draw the graphs of f , g , and h for x near 1.
(b) Explain how you can use the Squeeze Theorem to figure out $\lim_{x \rightarrow 1} g(x)$.