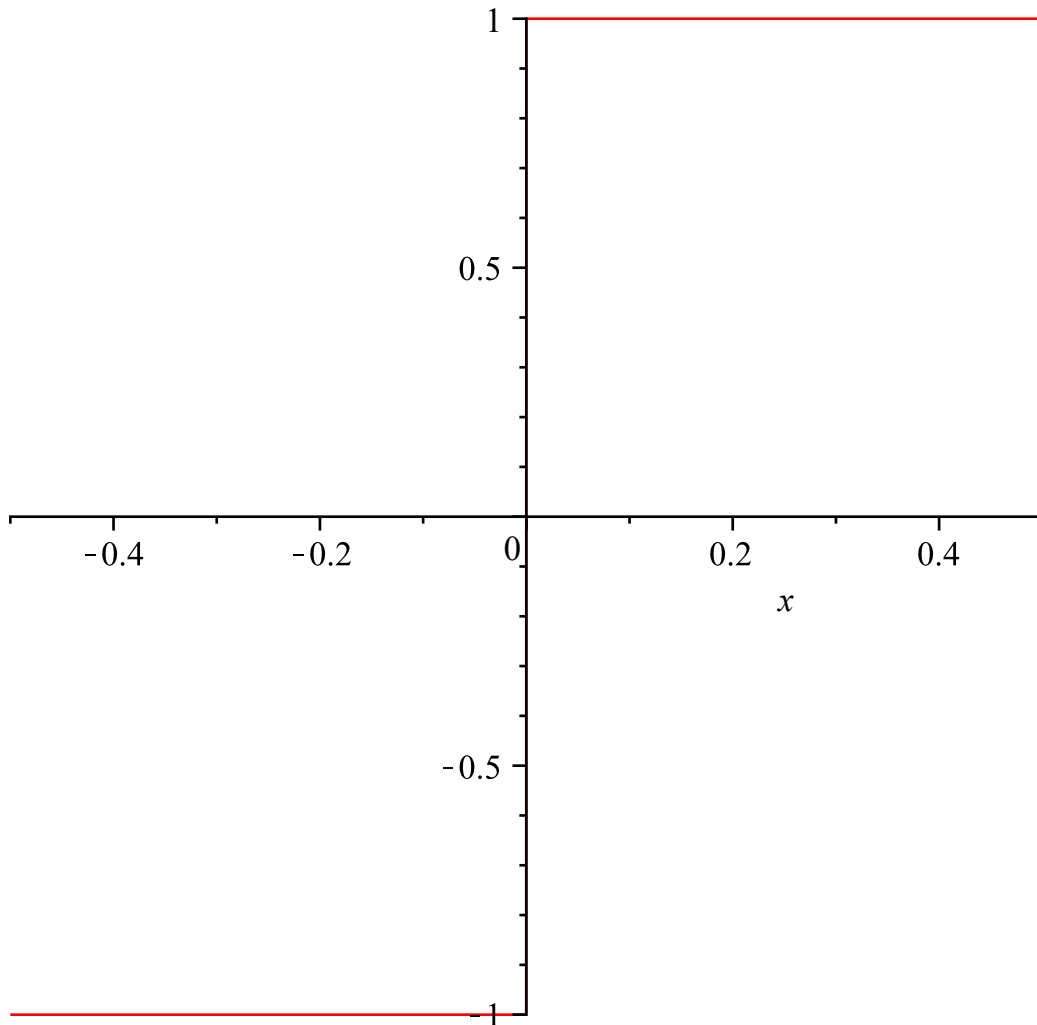


```
> f := piecewise(x < 0, -1, 1);
```

$$f := \begin{cases} -1 & x < 0 \\ 1 & \text{otherwise} \end{cases}$$

(1)

```
> plot(f, x=-0.5..0.5);
```



```
> b := proc(n)
2*(1-(-1)^n)/(Pi*n)
end proc;
```

```
> map(b, [seq(t, t=1..20)]);
```

```
 $\left[ \frac{4}{\pi}, 0, \frac{4}{3\pi}, 0, \frac{4}{5\pi}, 0, \frac{4}{7\pi}, 0, \frac{4}{9\pi}, 0, \frac{4}{11\pi}, 0, \frac{4}{13\pi}, 0, \frac{4}{15\pi}, 0, \frac{4}{17\pi}, 0, \frac{4}{19\pi}, 0 \right]$ 
```

(2)

```
> std_sum := proc(N)
local out, k;
out := 0;
for k from 1 to N do
out := out + b(k)*sin(2*Pi*k*x)
end do;
out
end proc;
```

```
> s5 := std_sum(5);
```

$$s5 := \frac{4 \sin(2 \pi x)}{\pi} + \frac{4}{3} \frac{\sin(6 \pi x)}{\pi} + \frac{4}{5} \frac{\sin(10 \pi x)}{\pi} \quad (3)$$

> s9 := std_sum(9);

$$s9 := \frac{4 \sin(2 \pi x)}{\pi} + \frac{4}{3} \frac{\sin(6 \pi x)}{\pi} + \frac{4}{5} \frac{\sin(10 \pi x)}{\pi} + \frac{4}{7} \frac{\sin(14 \pi x)}{\pi} + \frac{4}{9} \frac{\sin(18 \pi x)}{\pi} \quad (4)$$

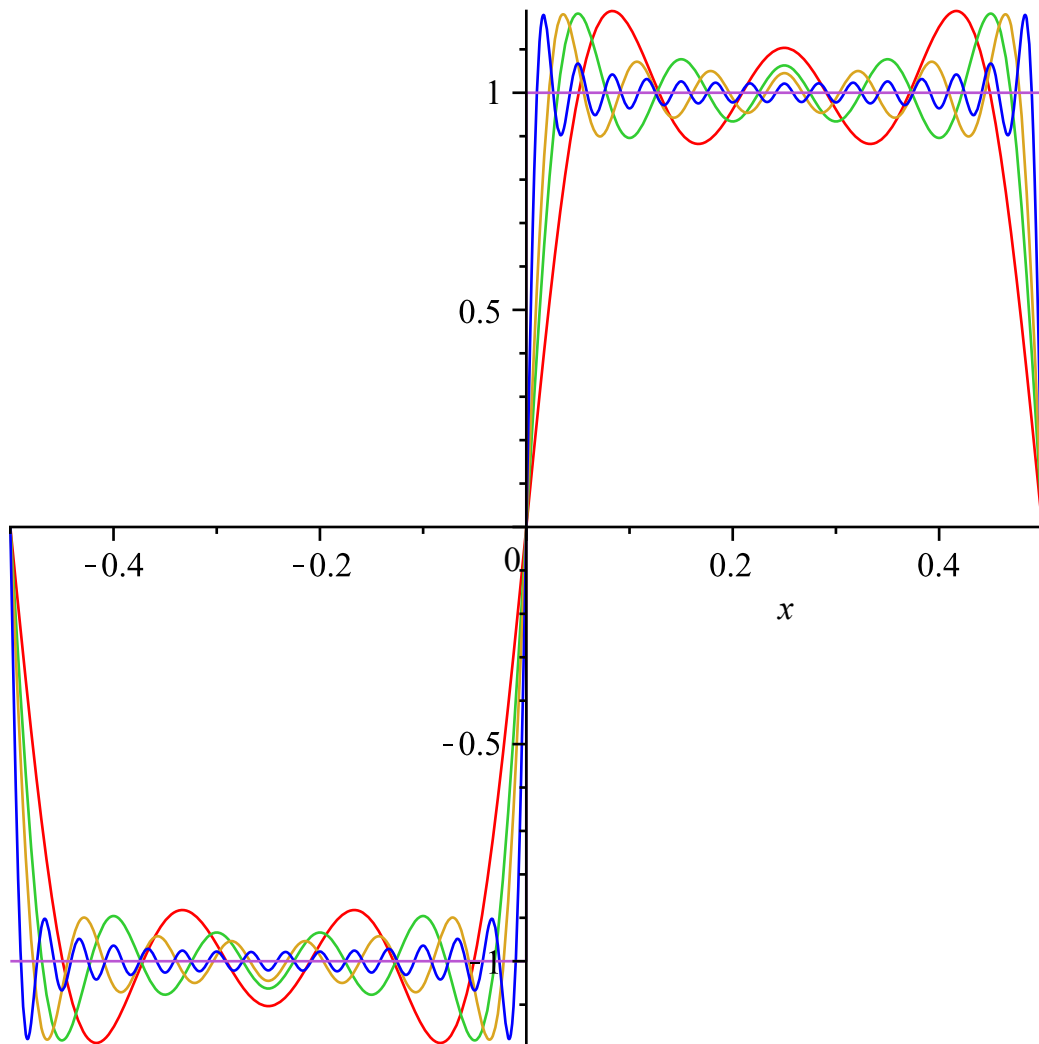
> s13 := std_sum(13);

$$s13 := \frac{4 \sin(2 \pi x)}{\pi} + \frac{4}{3} \frac{\sin(6 \pi x)}{\pi} + \frac{4}{5} \frac{\sin(10 \pi x)}{\pi} + \frac{4}{7} \frac{\sin(14 \pi x)}{\pi} + \frac{4}{9} \frac{\sin(18 \pi x)}{\pi} + \frac{4}{11} \frac{\sin(22 \pi x)}{\pi} + \frac{4}{13} \frac{\sin(26 \pi x)}{\pi} \quad (5)$$

> s29 := std_sum(29);

$$s29 := \frac{4 \sin(2 \pi x)}{\pi} + \frac{4}{3} \frac{\sin(6 \pi x)}{\pi} + \frac{4}{5} \frac{\sin(10 \pi x)}{\pi} + \frac{4}{7} \frac{\sin(14 \pi x)}{\pi} + \frac{4}{9} \frac{\sin(18 \pi x)}{\pi} + \frac{4}{11} \frac{\sin(22 \pi x)}{\pi} + \frac{4}{13} \frac{\sin(26 \pi x)}{\pi} + \frac{4}{15} \frac{\sin(30 \pi x)}{\pi} + \frac{4}{17} \frac{\sin(34 \pi x)}{\pi} + \frac{4}{19} \frac{\sin(38 \pi x)}{\pi} + \frac{4}{21} \frac{\sin(42 \pi x)}{\pi} + \frac{4}{23} \frac{\sin(46 \pi x)}{\pi} + \frac{4}{25} \frac{\sin(50 \pi x)}{\pi} + \frac{4}{27} \frac{\sin(54 \pi x)}{\pi} + \frac{4}{29} \frac{\sin(58 \pi x)}{\pi} \quad (6)$$

> plot({f,s5,s9,s13,s29},x=-0.5..0.5);



```

> cesaro_sum := proc(N)
local out, k;
out := 0;
for k from 1 to N-1 do
out := out + ((N-k)/N)*b(k)*sin(2*Pi*k*x)
end do;
out
end proc:

```

```

> sigma6 := cesaro_sum(6);

```

$$\sigma_6 := \frac{10}{3} \frac{\sin(2\pi x)}{\pi} + \frac{2}{3} \frac{\sin(6\pi x)}{\pi} + \frac{2}{15} \frac{\sin(10\pi x)}{\pi} \quad (7)$$

```

> sigma10 := cesaro_sum(10);

```

$$\sigma_{10} := \frac{18}{5} \frac{\sin(2\pi x)}{\pi} + \frac{14}{15} \frac{\sin(6\pi x)}{\pi} + \frac{2}{5} \frac{\sin(10\pi x)}{\pi} + \frac{6}{35} \frac{\sin(14\pi x)}{\pi} + \frac{2}{45} \frac{\sin(18\pi x)}{\pi} \quad (8)$$

```

> sigma14 := cesaro_sum(14);

```

(9)

$$\sigma_{14} := \frac{26}{7} \frac{\sin(2\pi x)}{\pi} + \frac{22}{21} \frac{\sin(6\pi x)}{\pi} + \frac{18}{35} \frac{\sin(10\pi x)}{\pi} + \frac{2}{7} \frac{\sin(14\pi x)}{\pi} \quad (9)$$

$$+ \frac{10}{63} \frac{\sin(18\pi x)}{\pi} + \frac{6}{77} \frac{\sin(22\pi x)}{\pi} + \frac{2}{91} \frac{\sin(26\pi x)}{\pi}$$

> sigma30 := cesaro_sum(30);

$$\sigma_{30} := \frac{58}{15} \frac{\sin(2\pi x)}{\pi} + \frac{6}{5} \frac{\sin(6\pi x)}{\pi} + \frac{2}{3} \frac{\sin(10\pi x)}{\pi} + \frac{46}{105} \frac{\sin(14\pi x)}{\pi} \quad (10)$$

$$+ \frac{14}{45} \frac{\sin(18\pi x)}{\pi} + \frac{38}{165} \frac{\sin(22\pi x)}{\pi} + \frac{34}{195} \frac{\sin(26\pi x)}{\pi} + \frac{2}{15} \frac{\sin(30\pi x)}{\pi}$$

$$+ \frac{26}{255} \frac{\sin(34\pi x)}{\pi} + \frac{22}{285} \frac{\sin(38\pi x)}{\pi} + \frac{2}{35} \frac{\sin(42\pi x)}{\pi} + \frac{14}{345} \frac{\sin(46\pi x)}{\pi}$$

$$+ \frac{2}{75} \frac{\sin(50\pi x)}{\pi} + \frac{2}{135} \frac{\sin(54\pi x)}{\pi} + \frac{2}{435} \frac{\sin(58\pi x)}{\pi}$$

> plot({f,sigma6,sigma10,sigma14,sigma30},x=-0.5..0.5);

